

Enhancing Model Poisoning Attacks to Byzantine-Robust Federated Learning via Critical Learning Periods

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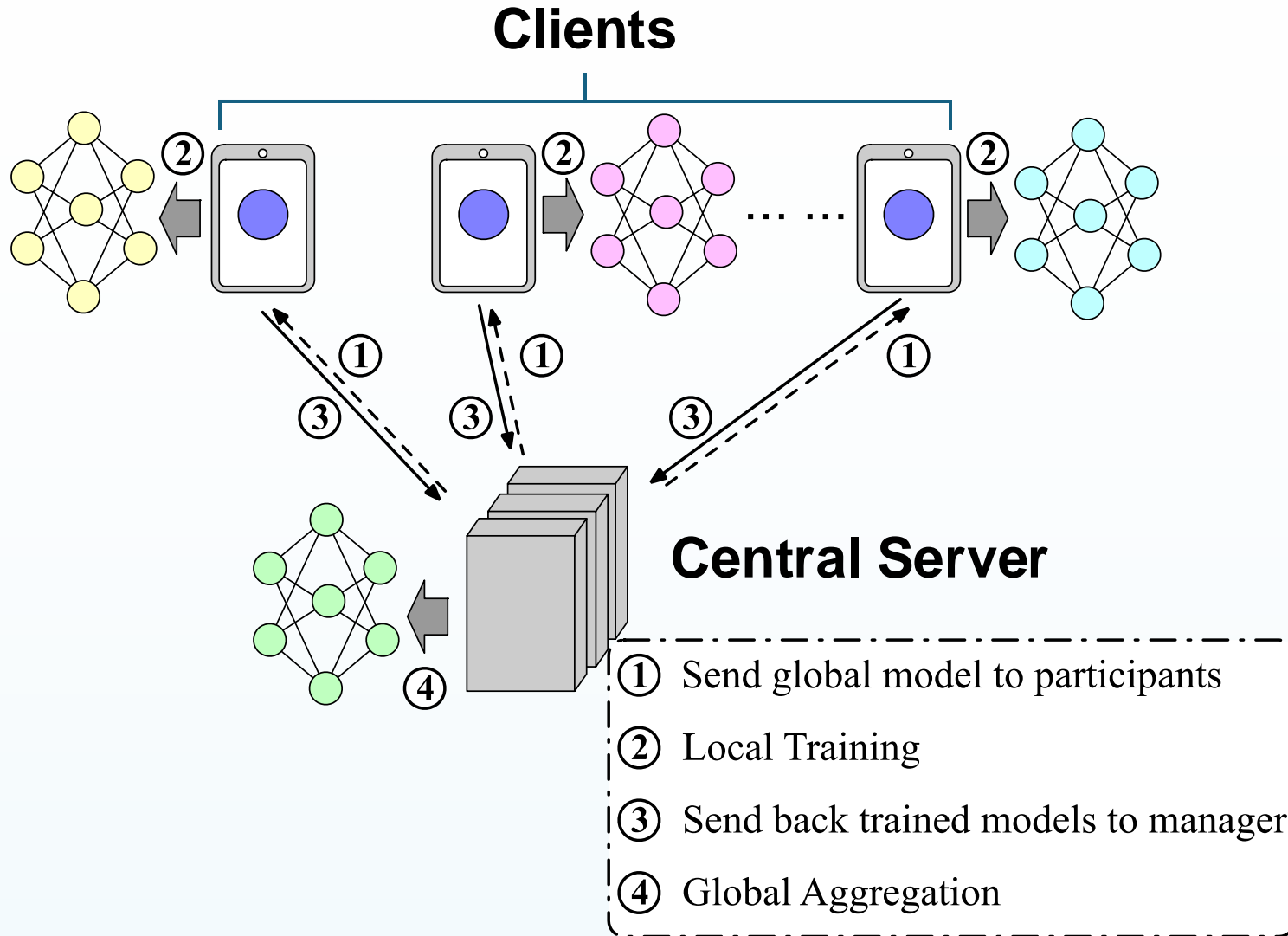
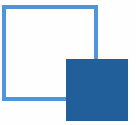
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I. Basics of Federated Learning





Goal

$$\min_{\mathbf{w} \in \mathbb{R}^d} \mathcal{L}(\mathbf{w}, D) := \sum_{i \in \mathcal{N}} \frac{|D_i|}{|D|} \mathcal{L}_i(\mathbf{w}, D_i)$$

where local loss $\mathcal{L}_i(\mathbf{w}, D_i)$

Local Training

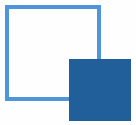
$$\mathbf{w}_i^{(t)}(k) \leftarrow \mathbf{w}_i^{(t)}(k-1) - \eta \nabla \mathcal{L}_i$$

where η is learning rate

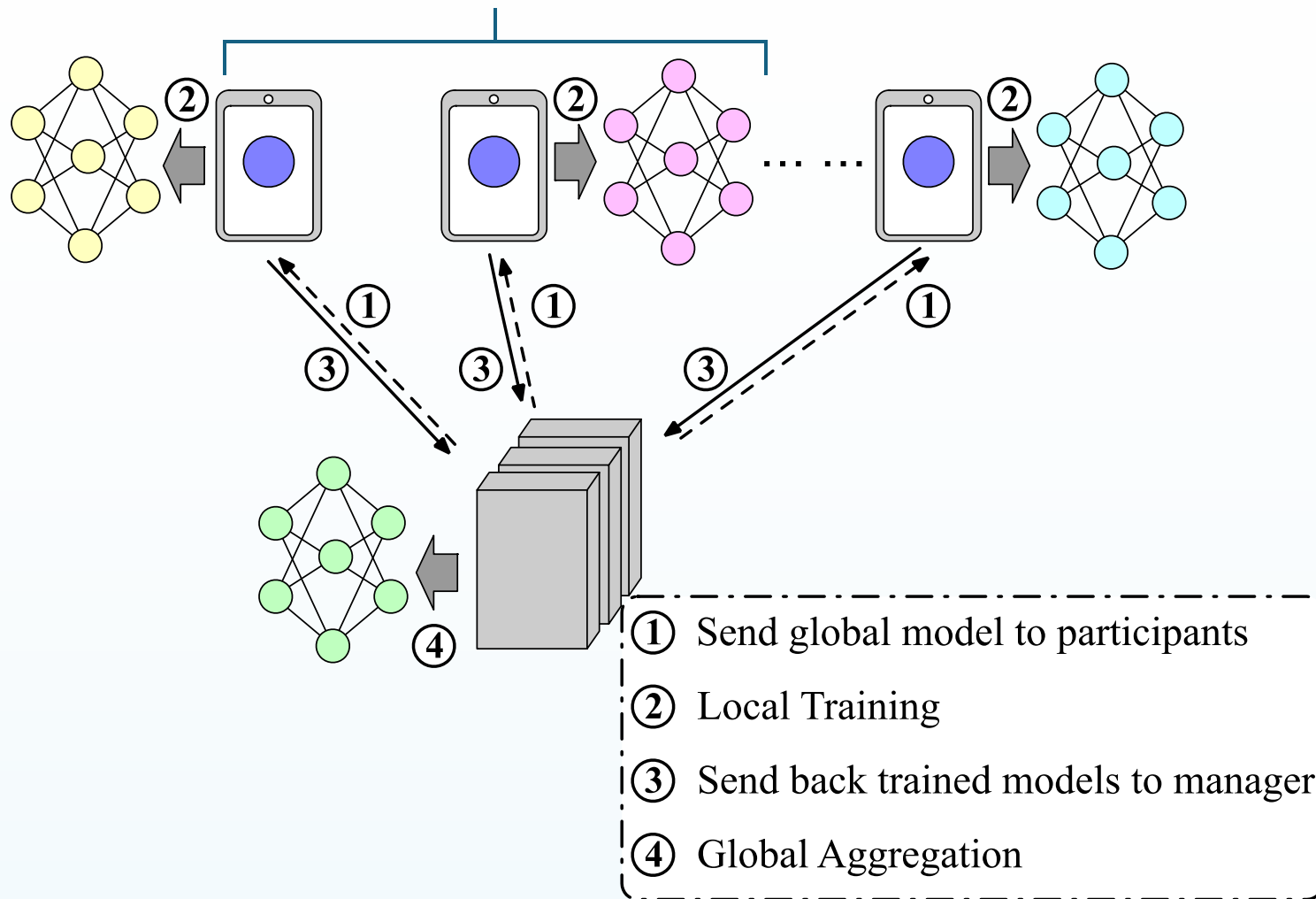
Global Aggregation

$$\mathbf{w}^{(t)} \leftarrow \sum_{i \in \mathcal{N}^{(t)}} \frac{|D_i|}{|\cup_{i \in \mathcal{N}^{(t)}} D_i|} \mathbf{w}_i^{(t)}(K)$$

Byzantine-robust Aggregation Rules on server



Attack



❑ Targeted Attack

- Minimize the accuracy on specific test inputs

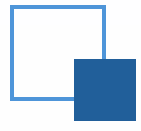
❑ Untargeted Attack

- Minimize the global model accuracy on any test input

❑ Defense

- Byzantine-robust methods on central server
- Detect and remove outliers
- Limit malicious updates' impacts

❖ **Attack:** degrade the global model accuracy by contributing malicious model updates



- ❑ **Fixed Attack Budget:** Utilizes a **constant number of malicious clients**, leading to a tradeoff between attack impact and budget
- ❑ **Uniform Attack Strategy:** Assumes **all training phases are equally important**, overlooking the significance of initial learning phases
- ❑ **Vulnerability to Defenses:** **Susceptible** to detection and mitigation by robust defenses (e.g., FLTrust, SparseFed)
- ❑ **Lack of Adaptiveness:** Fails to adjust the attack strategy based on ***critical learning periods***, missing the opportunity for maximum impact

What are Critical Learning Periods?

What are CL Periods?

WILLKOMMEN

欢迎

स्वागत

BIENVENIDA

WELCOME

BIENVENUE ようこそ

добро пожаловать

ترحيب

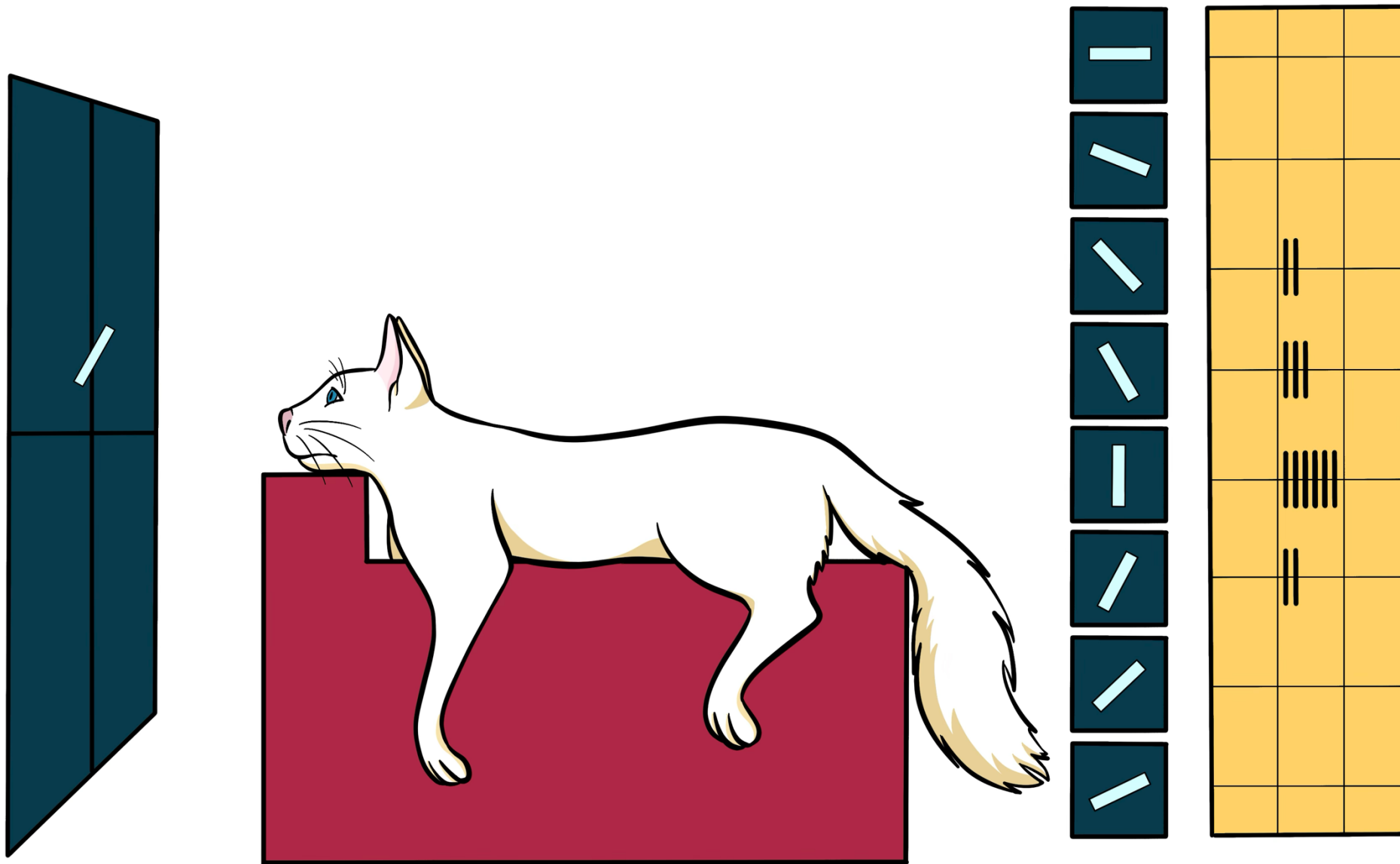
BEM-VINDO



What are CL Periods?

- **Two special cylinders**
 - Vertical/horizontal lines
- Kittens that were exposed to vertical lines for **the first few months since birth**
 - Only see vertical lines, but not horizontal ones—for the rest of their lives
 - And vice versa





<https://www.futurelearn.com/info/courses/research-methods-psychology-animal-models-to-understand-human-behaviour/0/steps/265398>

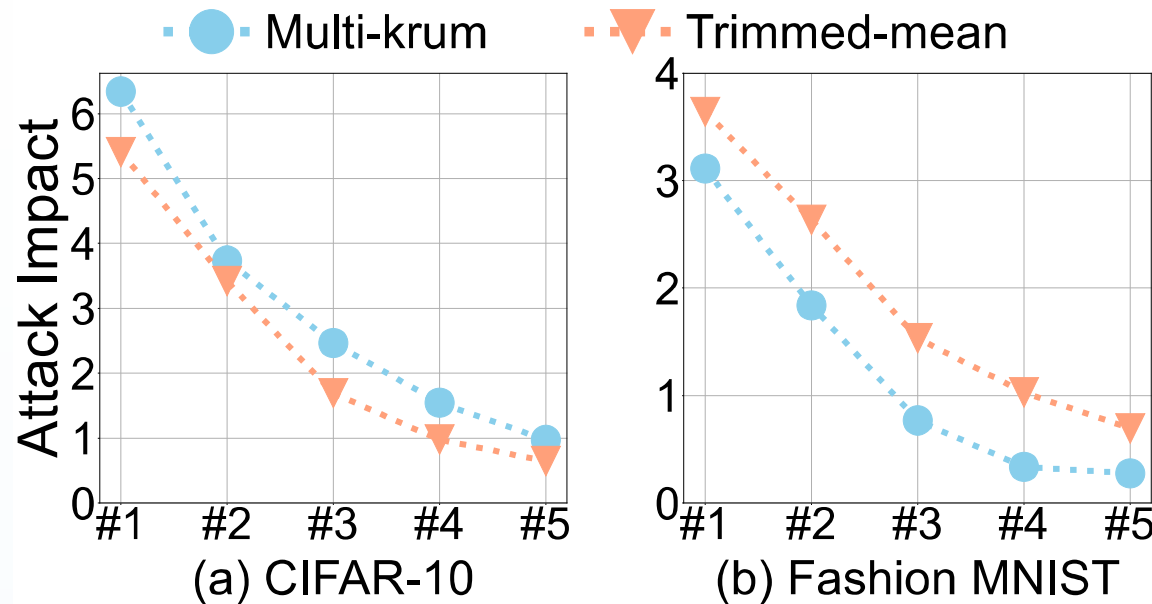


Figure 1: FL under model poisoning attacks exhibits CLP, where the Min-Max attack occurs in (#1) rounds 0-20; (#2) rounds 20-40; (#3) rounds 40-60; (#4) rounds 60-80; and (#5) rounds 80-100, respectively.

- Critical Learning Periods (CLP):** *Initial training phases in deep neural networks that have an irreversible impact on the model's final quality*

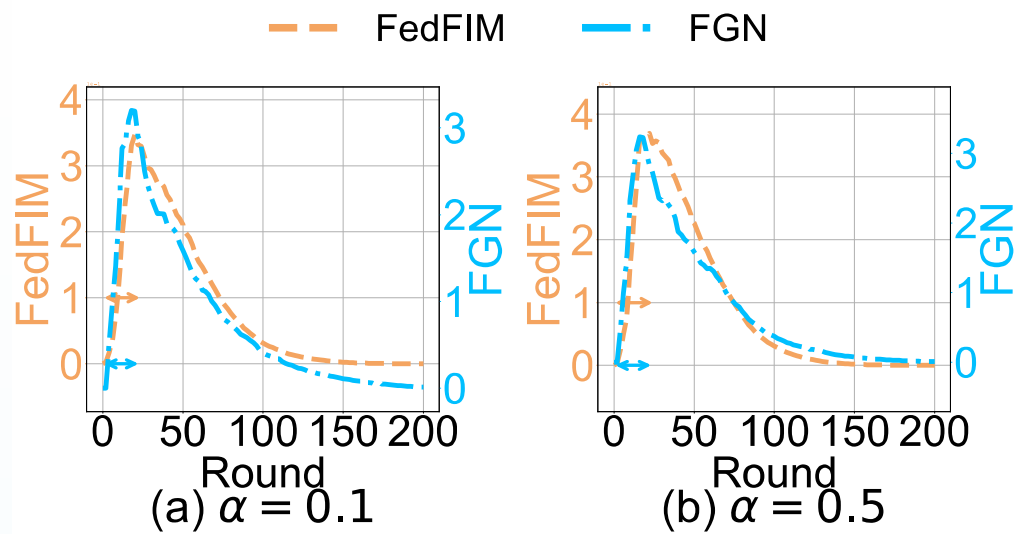


Figure 2: Detecting CLP via FGN and FedFIM, where the shade and double-arrows indicate identified CLP.

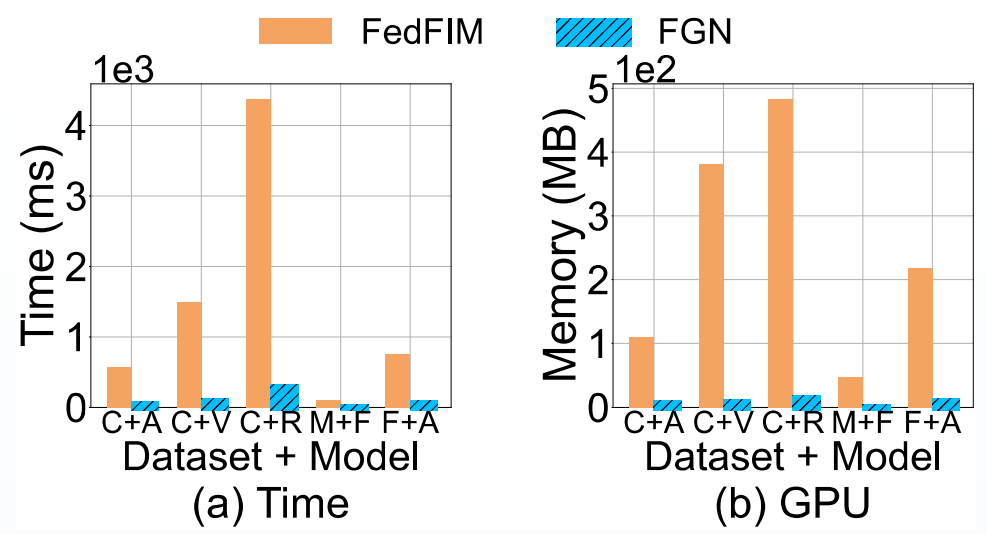


Figure 3: Computation time and memory consumption of FGN and FedFIM approach to detect CLP.

❑ Federated Gradient Norm (FGN):
 CLP is identified using the changes in the Federated Gradient Norm during training

❑ Why FGN?: FGN provides a computationally efficient and online method to detect CLP, allowing for adaptive adjustments in the attack strategy



❑ *A*-CLP (CLP-Aware Model Poisoning)

- **Adaptive Budget:** Dynamically adjusts the number of malicious clients
- **Optimized Strategy:** Increases attack budget during CLP for maximum impact, reducing it afterward to enhance efficiency
- **Improved Resilience:** Strengthens resistance against defenses like FLTrust

❑ GraSP (CLP-Aware Similarity-Based Attack)

- **Lightweight:** Uses a cosine similarity approach to craft malicious gradients
- **Approximate Deviations:** Deviates gradients based on similarity, without strictly following the global model's inverse direction
- **Superior Impact:** Achieves better attack performance

II. Design of \mathcal{A} -CLP



Algorithm 1 \mathcal{A} -CLP: CLP Aware Model Poisoning Attacks

```
1: for  $t = 0, 1, \dots, T - 1$  do
2:   if  $\frac{\text{FGN}(t) - \text{FGN}(t-1)}{\text{FGN}(t-1)} \geq \delta$  then
3:     The adversary invokes a larger number of malicious clients
       to share malicious gradients (e.g.,  $2m$ ) with the central
       server //More malicious clients during CLP
4:   else
5:     A smaller number of malicious clients is invoked to share
       malicious gradients (e.g.,  $m/2$ ) with the central server
       //Fewer malicious clients after CLP
6:   end if
7: end for
```

- ❑ **Concept:** \mathcal{A} -CLP adapts the number of malicious clients during federated learning rounds based on the identification of CLP
- ❑ **Key Insight:** Larger attack budgets are only required during the initial critical learning periods for maximum impact



$$M' = \left\lceil \frac{(N - M)m}{n - m} \right\rceil, \quad m \leq \left\lceil \frac{nM}{N} \right\rceil.$$

N denotes the total number of clients,

n represents the clients selected in each round

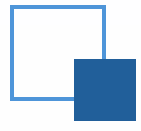
M is the total number of controlled clients

M' is the number of **activated clients**

m is the corresponding number of **selected malicious clients (we want to guarantee)**

M'	Method	$n = 16$	$n=32$	$n = 48$
$m = 0.0625n$	Equation (1)	7	7	7
	Simulation	7	7	7
$m = 0.125n$	Equation (1)	14	14	14
	Simulation	14	14	14
$m = 0.25n$	Equation (1)	32	32	32
	Simulation	32	32	32

Table 1: The number of malicious clients M' invoked by the adversary so as to guarantee that on average m malicious clients are selected by the server.



- ❑ **Datasets:** CIFAR-10, CIFAR-100, MNIST, Fashion-MNIST, Shakespeare
- ❑ **Models:** AlexNet, VGG-11, ResNet-18, LSTM
- ❑ **Baseline Attacks:** Fang, LIE, Min-Sum, Min-Max, MPHM
- ❑ **Settings:** Total number of clients $N = 128$ selected clients $n = 32$, controlled clients $M = 32$
- ❑ **Objective:** Evaluate the attack impact, budget, and resilience against different defense mechanisms

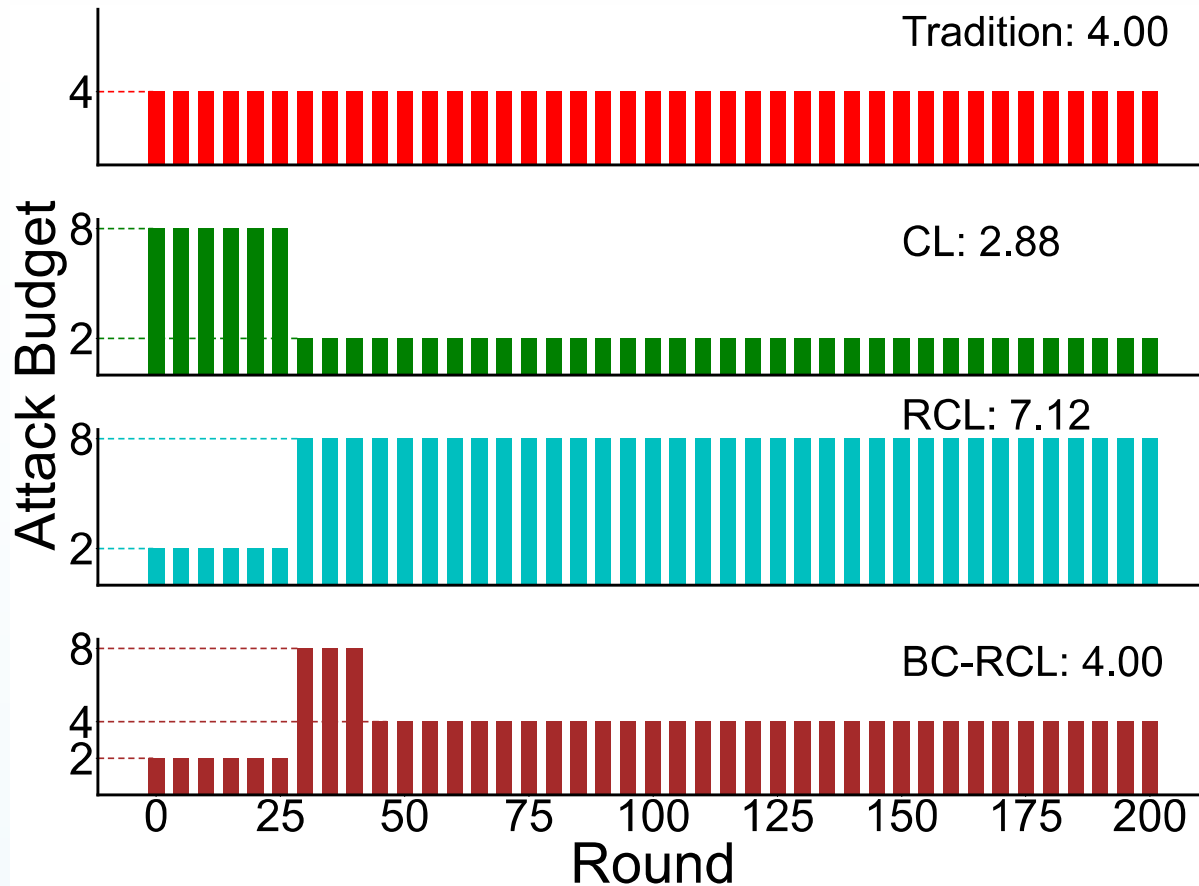
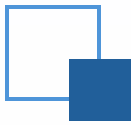


Figure 4: The attack budget: A fixed average attack budget of 4 per round.

- ❑ **Traditional**: Uses a fixed number of malicious clients throughout all training rounds
- ❑ **CL (CLP-Aware)**: Increases the number of malicious clients during CLP and reduces it after
- ❑ **RCL (Reverse CLP)**: Reduces malicious clients during CLP and increases them afterward
- ❑ **BC-RCL (Budget-Constrained RCL)**: Similar to RCL but with a fixed overall attack budget

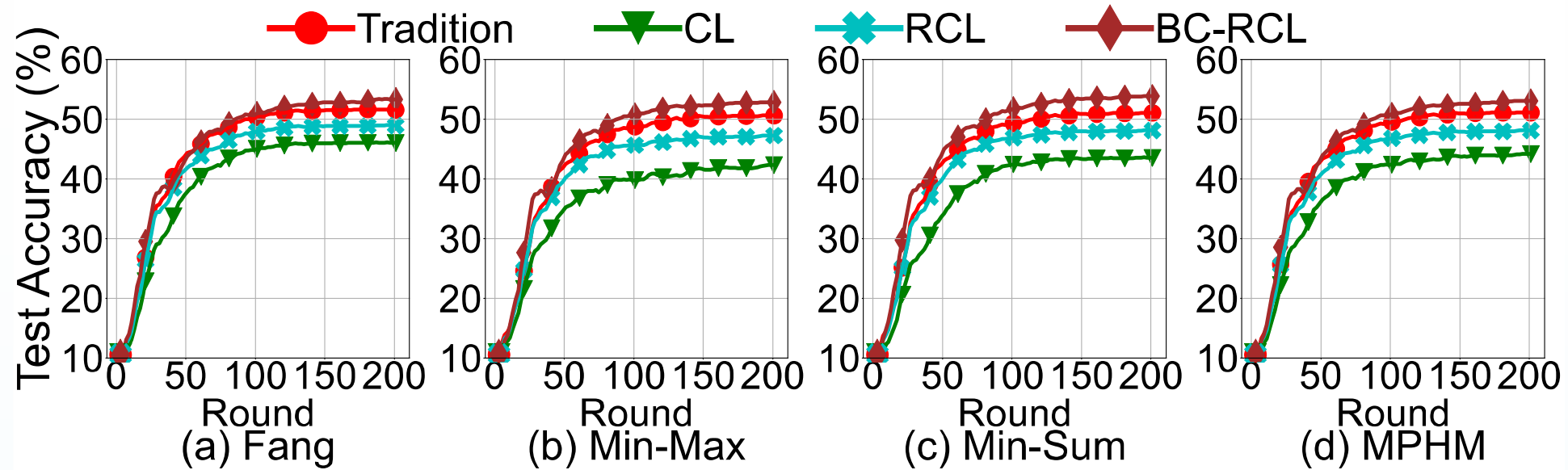


Figure 5: Comparisons of different CLP aware attacks to FL. All attacks *do not know the gradients on benign clients*.

- ❑ **\mathcal{A} -CLP (CL)** significantly **outperforms** traditional attacks, achieving **higher accuracy reduction** by dynamically targeting CLP
- ❑ **RCL** and **BC-RCL** show **limited impact** as they fail to fully leverage the CLP



Evaluations of Attack Impact

Dataset (Model)	Aggregation Rule	No Attack (Accuracy)	Fang		LIE		Min-Max		Min-Sum		MPHM		Label Flipping	
			Trad.	CL	Trad.	CL	Trad.	CL	Trad.	CL	Trad.	CL	Trad.	CL
CIFAR-10 (AlexNet)	Multi-krum [10]	57.57	10.40	20.02	5.73	11.86	12.03	26.47	11.32	24.37	11.19	23.27	3.23	7.94
	Bulyan [17]	56.34	9.40	20.69	7.50	12.99	7.98	20.90	6.53	16.95	8.15	20.73	4.89	10.54
	Trimmed-mean [59, 66]	57.33	10.32	22.44	7.36	17.23	9.50	22.85	8.35	19.44	8.91	21.37	6.19	12.05
	Median [59, 66]	55.46	11.73	22.62	10.89	18.44	9.10	20.48	7.91	18.44	9.03	20.14	6.95	13.04
	AFA [41]	57.89	6.99	11.81	2.98	7.41	9.27	19.05	7.73	14.83	8.81	17.32	2.01	5.30
CIFAR-10 (VGG-11)	Multi-krum [10]	62.63	9.13	16.03	6.24	12.82	9.94	17.94	9.50	18.07	9.72	18.03	3.12	4.36
	Bulyan [17]	63.37	15.16	22.53	13.46	19.56	14.91	21.85	14.54	21.52	14.88	21.69	7.13	11.60
	Trimmed-mean [59, 66]	62.90	11.62	18.88	11.20	17.02	13.14	20.89	10.09	20.95	12.53	20.34	5.54	11.08
	Median [59, 66]	60.13	15.23	23.58	12.80	15.98	15.05	23.00	14.38	23.34	14.49	23.56	5.44	7.67
	AFA [41]	62.75	7.21	10.58	6.26	8.55	8.54	11.55	7.87	11.09	8.19	11.41	4.43	6.18
CIFAR-100 (ResNet-18)	Multi-krum [10]	34.89	17.68	25.62	5.33	11.09	16.62	25.53	10.69	20.23	18.49	25.22	3.29	6.02
	Bulyan [17]	35.21	14.28	16.61	8.15	11.67	12.58	19.11	10.36	14.93	13.72	18.62	4.65	8.75
	Trimmed-mean [59, 66]	35.26	10.01	18.49	7.85	9.41	10.60	18.20	11.17	19.62	10.93	19.34	5.70	8.19
	Median [59, 66]	34.79	12.41	23.59	4.97	9.71	9.83	21.18	9.68	17.93	12.37	23.90	3.10	6.84
	AFA [41]	34.59	9.94	11.85	2.05	6.33	9.33	13.70	8.12	13.38	10.13	13.93	1.59	3.67
MNIST (FC)	Multi-krum [10]	97.02	1.59	2.06	0.26	0.96	1.51	2.32	1.47	2.25	1.49	2.30	0.04	0.72
	Bulyan [17]	97.21	1.36	1.88	0.84	1.18	1.32	2.14	1.23	2.06	1.28	2.09	0.34	1.02
	Trimmed-mean [59, 66]	97.24	1.49	2.05	0.24	0.93	1.35	2.28	1.35	2.23	1.32	2.27	0.08	0.62
	Median [59, 66]	96.93	1.51	2.03	0.31	1.00	1.31	2.15	1.25	2.12	1.27	2.16	0.08	0.57
	AFA [41]	97.20	1.27	1.70	0.13	0.89	1.28	2.06	1.28	2.08	1.29	2.10	0.02	0.52
Fashion MNIST (AlexNet)	Multi-krum [10]	83.24	5.97	11.05	3.51	6.30	5.06	15.05	4.64	12.10	5.80	15.37	2.08	2.69
	Bulyan [17]	83.12	7.79	20.58	3.95	7.42	6.80	13.24	5.51	12.88	7.95	20.34	1.62	3.97
	Trimmed-mean [59, 66]	83.53	6.10	9.39	4.46	11.62	5.21	8.75	4.93	8.57	6.02	11.77	2.66	3.42
	Median [59, 66]	81.81	5.34	8.88	5.84	10.65	4.27	8.25	4.14	8.72	5.49	9.21	1.23	2.66
	AFA [41]	83.97	4.04	6.46	2.96	5.09	4.91	9.49	3.62	7.57	4.86	9.30	2.26	3.91
Shakespeare (LSTM)	Multi-krum [10]	47.14	9.65	11.94	2.65	4.73	8.80	11.75	8.08	11.07	8.23	11.29	1.68	3.34
	Bulyan [17]	46.52	10.38	13.71	1.63	3.48	8.25	12.14	7.71	11.50	7.99	11.60	1.22	2.69
	Trimmed-mean [59, 66]	46.93	9.03	12.18	2.23	3.98	8.26	11.12	7.92	10.76	8.04	10.98	1.53	3.26
	Median [59, 66]	45.76	9.09	11.53	1.37	3.16	7.45	10.38	7.05	9.96	7.25	9.52	1.05	2.44
	AFA [41]	47.41	7.19	10.14	4.09	5.50	8.58	10.98	8.47	9.91	8.36	9.68	1.43	2.97

□ **Attack Impact:**

$$\frac{\text{pure accuracy} - \text{attack accuracy}}{\text{pure accuracy}} \times 100\%$$

□ \mathcal{A} -CLP improves effectiveness by up to **6.85x** compared to traditional attacks

□ Achieves a greater impact while using a **smaller** attack budget

Table 2: The attack impact for state-of-the-art model poisoning attack \mathcal{A} and the corresponding CLP aware attack \mathcal{A} -CLP under various threats using non-IID partitioned datasets when *benign gradients are unknown* to attack \mathcal{A} .

Dataset (Model)	Defense	Fang		Min-Max		Min-Sum		MPHM	
		Trad.	CL	Trad.	CL	Trad.	CL	Trad.	CL
CIFAR-10 (AlexNet)	FLTrust	4.74	10.35	5.21	12.79	5.57	11.76	6.13	13.26
	SparseFed	6.84	11.73	6.32	12.61	6.22	12.46	7.03	12.68
	cosDefense	5.71	11.40	6.35	13.47	5.96	12.56	6.15	13.22
	FLAIR	6.57	12.53	7.27	13.81	8.03	14.13	7.53	14.01
	LeadFL	6.31	10.06	5.12	9.96	6.20	11.49	6.36	11.60
CIFAR-10 (VGG-11)	FLTrust	1.57	2.85	1.30	3.23	1.74	2.25	1.57	2.77
	SparseFed	2.71	4.63	2.60	4.42	2.57	4.02	3.01	4.88
	cosDefense	3.07	4.52	2.42	4.64	3.41	4.55	3.43	4.74
	FLAIR	2.86	4.25	3.05	4.96	4.01	5.04	3.76	4.79
	LeadFL	1.31	2.43	0.88	2.65	0.73	2.15	1.18	2.86
CIFAR-100 (ResNet-18)	FLTrust	3.10	4.49	2.45	5.19	2.43	5.47	2.99	5.73
	SparseFed	3.32	6.25	2.64	5.01	2.95	5.39	3.21	5.57
	cosDefense	3.39	5.42	4.51	5.56	3.62	5.85	5.39	6.45
	FLAIR	3.38	4.97	4.94	6.25	5.20	5.96	6.25	7.10
	LeadFL	1.85	3.55	0.97	3.95	0.82	3.72	2.19	4.34
MNIST (FC)	FLTrust	1.33	1.66	1.37	2.10	1.31	2.03	1.39	2.16
	SparseFed	1.22	1.65	1.12	1.81	1.53	1.79	1.60	1.84
	cosDefense	1.09	1.78	1.48	2.05	1.20	1.94	1.37	2.00
	FLAIR	1.28	1.58	1.01	1.93	1.24	2.07	1.18	2.05
	LeadFL	1.23	1.63	1.07	1.99	1.19	2.08	1.30	2.03
Fashion MNIST (AlexNet)	FLTrust	2.93	5.80	3.28	6.82	3.82	7.63	3.60	7.21
	SparseFed	3.25	5.35	2.56	4.41	2.51	5.39	3.06	4.76
	cosDefense	3.12	7.45	3.36	7.85	2.99	6.77	3.61	8.09
	FLAIR	3.48	7.32	3.72	7.58	3.92	7.86	4.17	8.13
	LeadFL	3.34	5.50	3.41	5.85	2.89	5.12	3.34	5.91
Shakespeare (LSTM)	FLTrust	4.43	5.58	5.41	7.24	5.74	7.05	5.64	7.38
	SparseFed	5.20	7.25	6.04	8.22	6.38	8.54	6.34	8.81
	cosDefense	5.31	6.94	5.35	7.78	6.05	7.58	5.78	7.74
	FLAIR	6.08	7.20	5.97	6.96	6.94	7.75	5.87	7.09
	LeadFL	4.05	6.57	5.12	7.89	4.39	7.41	4.78	8.16

Table 4: Attack impacts of \mathcal{A} and \mathcal{A} -CLP defended by FLTrust, SparseFed, cosDefense, FLAIR and LeadFL.

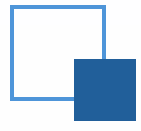
Attack Impact:

$$\frac{\text{pure accuracy} - \text{attack accuracy}}{\text{pure accuracy}} \times 100\%$$

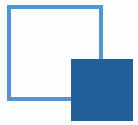
- Demonstrates **stronger resistance** against defenses (e.g., FLTrust, SparseFed), enhancing attack success by up to 2x
- Properly leveraging CLP with adaptive client selection significantly **boosts** the attack's **performance**

III. Design of GraSP





- ❑ **High Complexity of Existing Attacks:** Traditional model poisoning attacks are computationally intensive and complex
- ❑ **CLP Vulnerabilities:** Small gradient errors during CLP have a lasting impact, providing a window for more effective attacks
- ❑ **Need for Difference:** Current methods + \mathcal{A} -CLP produce very similar malicious updates, easily to be detected
- ❑ **GraSP's Goal:** Introduce a lightweight, similarity-based attack that maximizes impact with minimal computational effort, targeting the most vulnerable training phases



□ **Malicious local model** is calculated as:

$$\tilde{\mathbf{w}}_i(t) := \mathbf{w}_i(t) - \eta \lambda_i \mathbf{s}_t,$$

\mathbf{w} represents the model parameters

η is the learning rate

\mathbf{s}_t is the update direction at the t -th training round, which is estimated by using received local updates.

Model poisoning makes the model in the opposite direction of current update.



LEMMA 1. Suppose that λ_i is the changing direction to craft malicious gradient of the malicious client i , $\forall i = 1, \dots, m^{CLP}$. Then for any given attack threshold τ , the value of λ_i satisfies

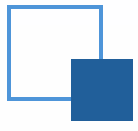
$$\lambda_i = \frac{\langle \mathbf{g}(t), \mathbf{g}_i(t) \rangle - \tau \|\mathbf{g}(t)\| \|\tilde{\mathbf{g}}(t)\|}{\mathbf{g}(t)^\top \mathbf{s}(t)}, \quad \forall i = 1, \dots, m^{CLP}. \quad (9)$$

$\mathbf{g}(t)$ is the estimated global update

$\tilde{\mathbf{g}}(t)$ is the **calculated targeted malicious global update**

$\mathbf{g}_i(t)$ represents the update of client i .

- Each client uses a **unique λ_i** to manipulate its local update. By **coordinating** their efforts, malicious clients make the attack harder to detect by defenses like FLTrust



□ The **targeted malicious global update** is calculated as:

$$\tilde{\mathbf{g}}(t) = \mathbf{g}(t) + \lambda \mathbf{s}(t)$$

where $\mathbf{g}(t) = \frac{1}{n} \sum_{i=1}^n \mathbf{g}_i(t)$, λ is solved by using the below proposition.

PROPOSITION 1. *Suppose that λ is the changing direction to craft gradients of m^{CLP} malicious clients based on the cosine similarity. For any given attack threshold τ , the value of λ is*

$$\lambda = \frac{-z - \sqrt{z^2 - 4xy}}{2x}, \quad (8)$$

where $x = (\mathbf{g}(t)^\top \mathbf{s}(t))^2 - \tau^2 \|\mathbf{g}(t)\|^2 \cdot \|\mathbf{s}(t)\|^2$, $y = (1 - \tau^2) \cdot \|\mathbf{g}(t)\|^4$,
and $z = 2(\tau^2 - 1) \|\mathbf{g}(t)\|^2 \cdot \mathbf{g}(t)^\top \mathbf{s}(t)$.

□ τ is the attack degree predefined by the attacker; in this work, it is set to 0.1.



Dataset (Model)	Attack	FLTrust	SparseFed	cosDefense	FLAIR	LeadFL
CIFAR-10 (AlexNet)	Best \mathcal{A}^* -CLP	13.26	12.68	13.47	14.13	11.60
	GraSP	13.98	14.21	14.98	15.14	13.33
CIFAR-10 (VGG-11)	Best \mathcal{A}^* -CLP	3.23	4.88	4.74	5.04	2.86
	GraSP	4.68	5.60	6.42	5.89	3.98
CIFAR-100 (ResNet-18)	Best \mathcal{A}^* -CLP	5.73	6.25	6.45	7.10	4.34
	GraSP	6.83	7.33	8.67	7.10	6.61
MNIST (FC)	Best \mathcal{A}^* -CLP	2.16	1.84	2.05	2.07	2.08
	GraSP	2.50	2.35	3.34	2.88	2.66
F. MNIST (AlexNet)	Best \mathcal{A}^* -CLP	7.63	5.39	8.09	8.13	5.91
	GraSP	7.95	6.74	9.42	8.57	7.19
Shakespeare (LSTM)	Best \mathcal{A}^* -CLP	7.38	8.81	7.78	7.75	8.16
	GraSP	8.23	10.23	9.84	8.59	9.40

Table 6: Attack impacts of GraSP and \mathcal{A}^* -CLP when defended by FLTrust, SparseFed, cosDefense, FLAIR and LeadFL under various threat models using non-IID partitioned datasets.

- Both demonstrate significantly **improved resilience** against advanced defenses (e.g., FLTrust, SparseFed, FLAIR).
- **GraSP** outperforms \mathcal{A} -CLP in most of scenarios, indicating its **strong adaptability** to defensive measures
- The similarity-based approach in GraSP leads to **sustained attack success**, especially during critical learning periods.

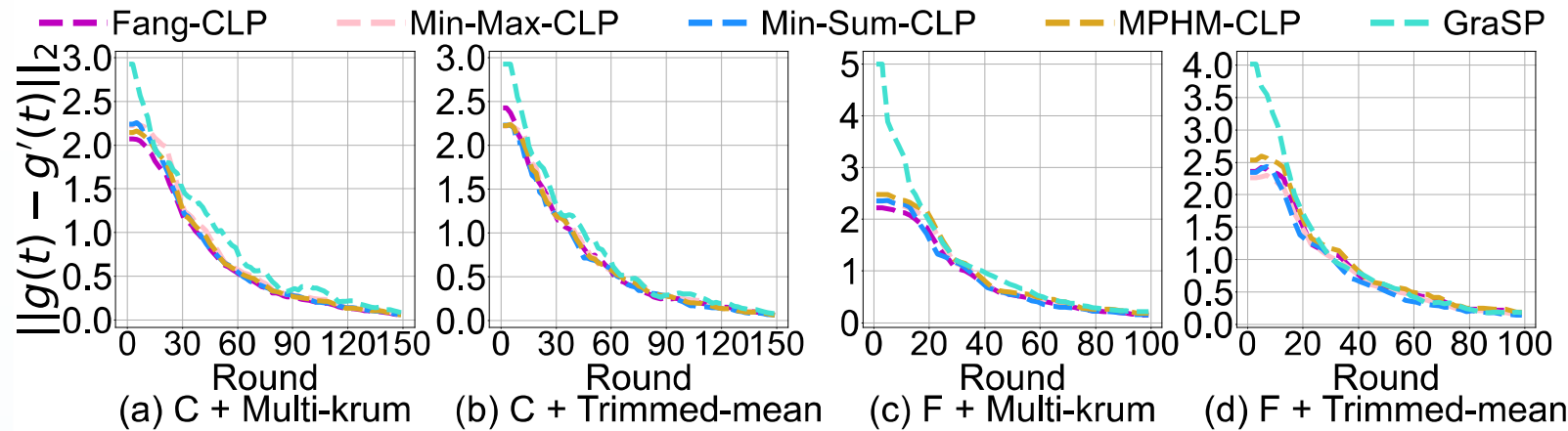


Figure 16: The ℓ_2 -norm of gradient magnitude different of CLP augmented attacks when *benign gradients are unknown* to the adversary, where “C” and “F” stands for CIFAR-10 and Fashion-MNIST datasets, respectively.

- GraSP shows **higher gradient magnitudes** during Critical Learning Periods (CLP), resulting in a greater impact on the global model
- Uses cosine similarity to target directions that most disrupt model updates, enabling **faster** and more **effective** gradient adjustments

IV. Conclusions



□ Defending Against \mathcal{A} -CLP:

- **Simple Approach:** Increase the number of participating clients during CLP to dilute the impact of malicious updates
- **Limitation:** Results in high communication costs and an increased attack budget

□ Defending Against GraSP:

- **Layer-Based Similarity:** Calculate gradient similarity across clients at specific layers to identify anomalies
- **Anomaly Detection:** Inspired by methods like AFA and cosDefense, potential malicious clients are excluded from model aggregation during CLP for stricter protection



□ Key Contributions

- Proposed **\mathcal{A} -CLP** and **GraSP**, adaptive attacks leveraging Critical Learning Periods (CLP) for greater impact
- Introduced the **FGN metric** for efficient, privacy-preserving CLP detection

□ Main Findings

- **\mathcal{A} -CLP** enhances attack success, achieving up to 6.85x more impact than traditional methods by adjusting malicious client numbers
- **GraSP** uses similarity-based strategies for effective gradient deviations with lower computational costs, outperforming current attacks



GitHub Repo:

<https://github.com/GYan58/RAID-2024-CLP>



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